

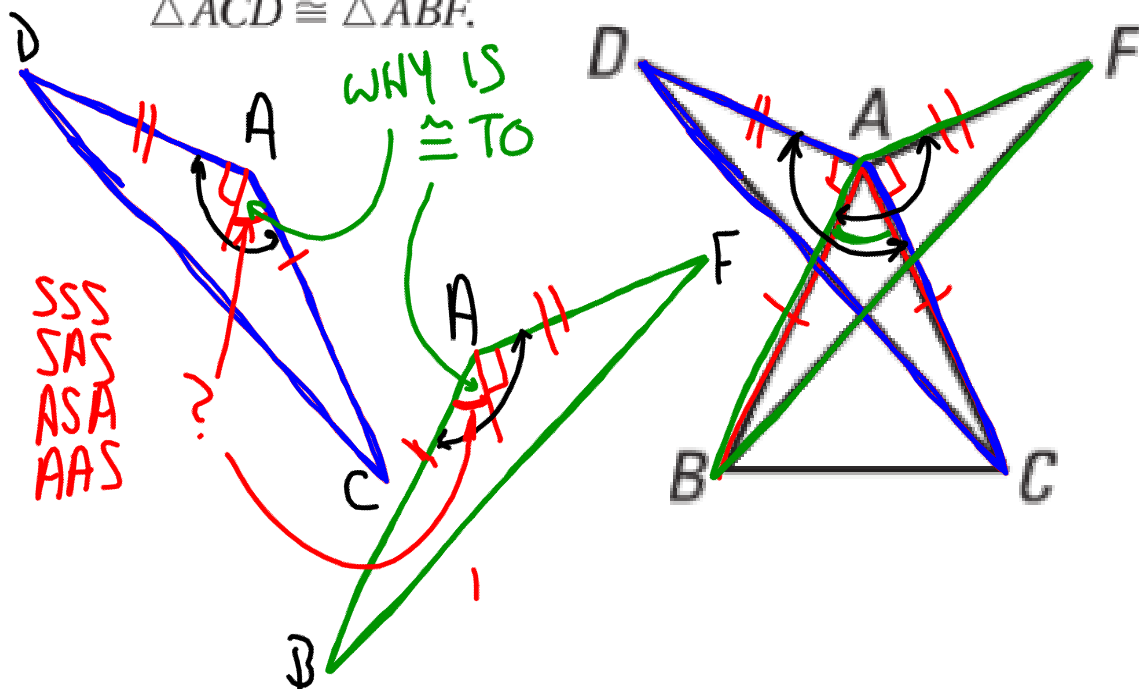
## 10/08/13 Agenda

- Warm Up
- Review Homework - Worksheet 7
- Section 4.4 - HL Congruency
- Start Homework
  - Worksheet 8 - HL Congruency

Homework out!

Warm Up:

**CHALLENGE** Suppose  $\overline{AB} \cong \overline{AC}$ ,  $\overline{AD} \cong \overline{AF}$ ,  $\overline{AD} \perp \overline{AB}$ , and  $\overline{AF} \perp \overline{AC}$ . Explain why you can conclude that  $\triangle ACD \cong \triangle ABF$ .

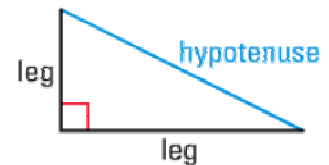


## Section 4.4 - HL Congruency

## Target 4E & 4F

Goal: Prove triangles congruent using HL.

**RIGHT TRIANGLES** In a right triangle, the sides adjacent to the right angle are called the **legs**. The side opposite the right angle is called the **hypotenuse** of the right triangle.



HL:  
(Hypotenuse,  
Leg)

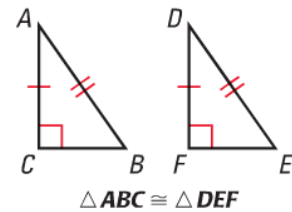
### THEOREM

*For Your Notebook*

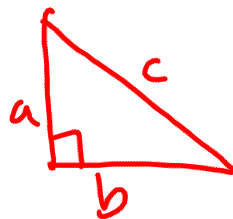
#### THEOREM 4.5 Hypotenuse-Leg (HL) Congruence Theorem

If the hypotenuse and a leg of a right triangle are congruent to the hypotenuse and a leg of a second right triangle, then the two triangles are congruent.

*Proofs:* Ex. 37, p. 439; p. 932



We usually need three congruent sides to prove triangles congruent, Why do you think, in this special case, we only need two congruent sides?



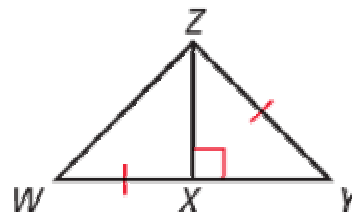
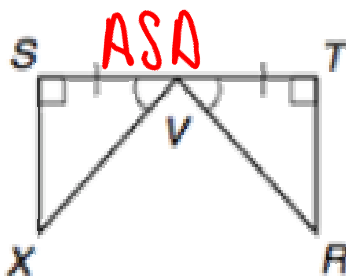
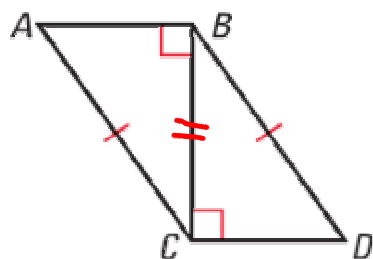
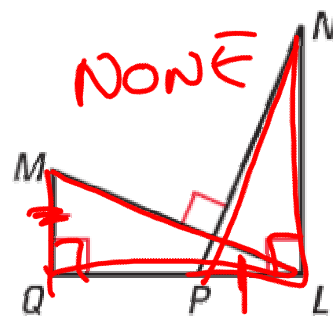
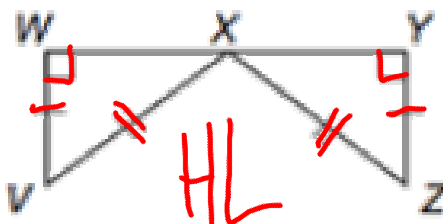
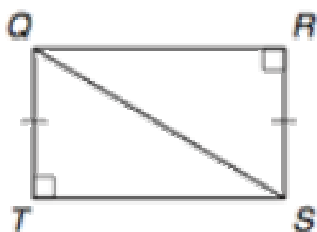
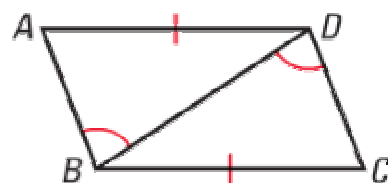
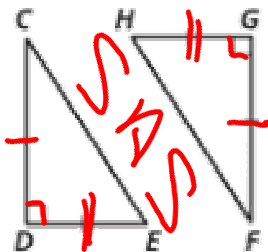
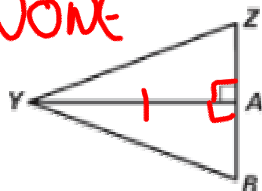
$$a^2 + b^2 = c^2$$

## Section 4.4 - HL Congruency

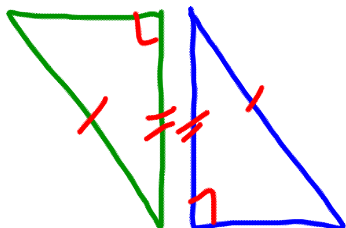
## Target 4E & 4F

Example: Decide what reason the triangles are congruent  
(SSS, SAS, ASA, AAS, HL, or None)

NONE



HL



NONE

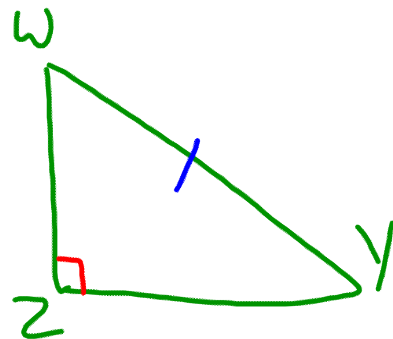
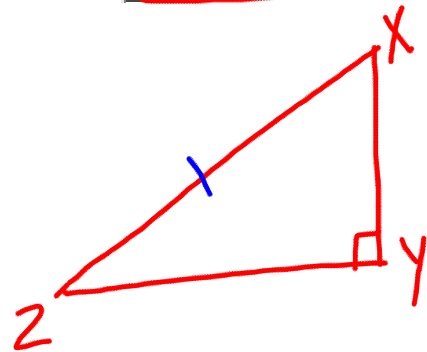
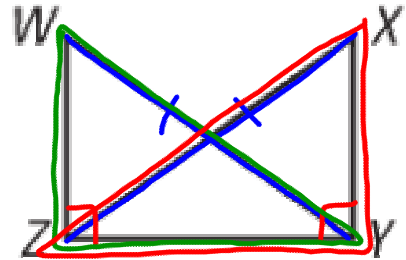
# Section 4.4 - HL Congruency

## Target 4E & 4F

Write a proof.

**GIVEN**  $\triangleright \overline{WY} \cong \overline{XZ}, \overline{WZ} \perp \overline{ZY}, \overline{XY} \perp \overline{ZY}$

**PROVE**  $\triangleright \triangle WYZ \cong \triangle XZY$



$$1. \overline{WY} \cong \overline{XZ}$$

$$\overline{WZ} \perp \overline{ZY}$$

$$\overline{XY} \perp \overline{ZY}$$

1. GIVEN

2.  $\angle WZY$  and  $\angle XYZ$  ARE  
 $\perp$

2. PROP OF  
 $\perp$  LINES

$$3. \angle WZY \cong \angle XYZ$$

3. ALL  $\perp$   $\angle$ s  
 $\cong$

$$4. \overline{ZY} \cong \overline{ZY}$$

4. REFLEXIVE PROP.

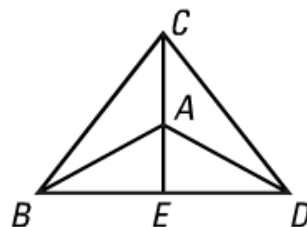
$$5. \triangle WZY \cong \triangle XZY$$

5. HL

## Section 4.4 - HL Congruency

## Target 4E & 4F

In the diagram,  $\overline{CE} \perp \overline{BD}$  and  $\angle CAB \cong \angle CAD$ .  
Write a flow proof to show  $\triangle ABE \cong \triangle ADE$ .

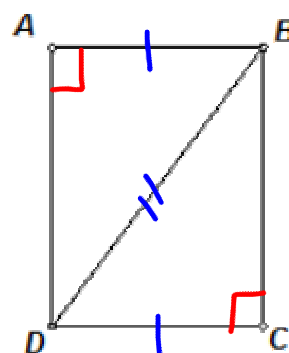
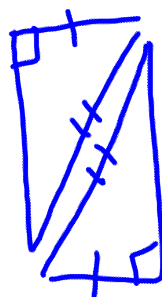


## Section 4.4 - HL Congruency

## Target 4E & 4F

Given:  $\overline{AB} \perp \overline{AD}$ ,  $\overline{BC} \perp \overline{DC}$ ,  $\overline{AB} \cong \overline{DC}$

Prove:  $\triangle DAB \cong \triangle BCD$



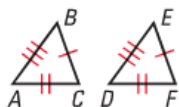
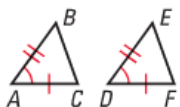


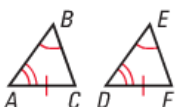
## Proving Triangle Congruency - Summary

### CONCEPT SUMMARY

*For Your Notebook*

#### Triangle Congruence Postulates and Theorems

You have learned five methods for proving that triangles are congruent.

SSS	SAS	HL (right $\triangle$ only)	ASA	AAS
 <p>All three sides are congruent.</p>	 <p>Two sides and the included angle are congruent.</p>	 <p>The hypotenuse and one of the legs are congruent.</p>	 <p>Two angles and the included side are congruent.</p>	 <p>Two angles and a (non-included) side are congruent.</p>